

# Chapter 3

## Parallel and Perpendicular Lines

### Study Guide

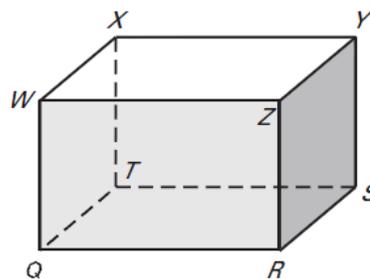
<p><b>3.1 Identify Pairs of Lines/Angles</b></p> <p style="text-align: center;">           Parallel Lines            Parallel Postulate            Perpendicular Postulate            Skew Lines            Parallel Planes            Diagram with a cube/box            Transversals            Angles formed by transversals              Corresponding Angles              Alternate Interior Angles              Alternate Exterior Angles              Consecutive Interior- (Same Side Interior) Angles         </p>	<p><b>3.2- Parallel Lines and Transversals</b></p> <p><b>**Know which angles are congruent and supplementary</b></p> <p style="text-align: center;">           Corresponding Angles Postulate            Alternate Interior Angles Theorem            Alternate Exterior Angles Theorem            Consecutive Interior- (Same Side Interior) Angles Theorem         </p> <p><b>**Know more difficult problems with multiple lines, systems of equations and factoring! (we had 2 worksheets on this!)</b></p>
<p><b>3.3 Proving Lines Parallel</b></p> <p><b>**Converses used to show lines are PARALLEL</b></p> <p style="text-align: center;">           Corresponding Angles Converse            Alternate Interior Angles Converse            Alternate Exterior Angles Converse            Consecutive Interior- (Same Side Interior) Angles Converse            Transitive Property of Parallel Lines         </p> <p><b>**Don't Forget About: Linear Pairs- Supplementary Vertical Angles- Congruent</b></p>	<p><b>3.6 Perpendicular Lines</b></p> <p>Theorem 3.8- Two lines intersect to form a linear pair of congruent angles, then the lines are perpendicular</p> <p style="text-align: center;">Theorem 3.9- If 2 lines are perpendicular, then they intersect to form 4 right angles</p> <p>Right Angle Pair Theorem (3.10)- Two angles that make a right angle pair are complementary</p> <p>Perpendicular Transversal Theorem- If a transversal is perpendicular to one of two parallel lines, then it is perpendicular to the other</p> <p>Lines Perpendicular to a Transversal Theorem- If two lines are perpendicular to the same line, then they are perpendicular to each other</p>

**Part I: Circle the word that best completes the sentence.**

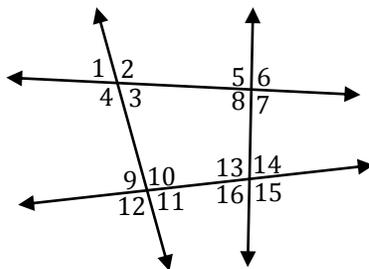
1. If two lines are parallel, then they (ALWAYS.....SOMETIMES.....NEVER) intersect.
2. If one line is skew to another, then they are (ALWAYS.....SOMETIMES.....NEVER) coplanar.
3. If two lines intersect, then they are (ALWAYS.....SOMETIMES.....NEVER) perpendicular.
4. If two lines are coplanar, then they are (ALWAYS.....SOMETIMES.....NEVER) parallel.
5. If two lines are cut by a transversal such that the alternate interior angles are (CONGRUENT.....COMPLEMENTARY.....SUPPLEMENTARY), then the lines are parallel.
6. If two lines are cut by a transversal such that the consecutive interior angles are (CONGRUENT.....COMPLEMENTARY.....SUPPLEMENTARY), then the lines are parallel.
7. If two lines are cut by a transversal such that the corresponding angles are (CONGRUENT.....COMPLEMENTARY.....SUPPLEMENTARY), then the lines are parallel.

**Part II: Think of each segment in the diagram as part of a line. Complete the statement with PARALLEL, SKEW, or PERPENDICULAR.**

1.  $\overrightarrow{WZ}$  and  $\overrightarrow{ZR}$  are \_\_\_\_\_
2.  $\overrightarrow{WZ}$  and  $\overrightarrow{ST}$  are \_\_\_\_\_
3.  $\overrightarrow{QT}$  and  $\overrightarrow{YS}$  are \_\_\_\_\_
4. Plane WZR and Plane SYZ are \_\_\_\_\_
5. Plane RQT and Plane YXW are \_\_\_\_\_



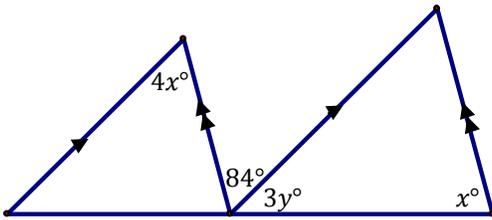
**Part III: Classify the angle pair as corresponding angles, alternate interior angles, alternate exterior angles, same side (consecutive) interior angles, vertical angles, linear pair, or none.**



- |                                      |                                       |
|--------------------------------------|---------------------------------------|
| 1. $\angle 1$ and $\angle 5$ _____   | 2. $\angle 4$ and $\angle 6$ _____    |
| 3. $\angle 5$ and $\angle 16$ _____  | 4. $\angle 16$ and $\angle 10$ _____  |
| 5. $\angle 10$ and $\angle 12$ _____ | 6. $\angle 11$ and $\angle 16$ _____  |
| 7. $\angle 12$ and $\angle 14$ _____ | 8. $\angle 4$ and $\angle 14$ _____   |
| 9. $\angle 7$ and $\angle 13$ _____  | 10. $\angle 12$ and $\angle 5$ _____  |
| 11. $\angle 6$ and $\angle 7$ _____  | 12. $\angle 10$ and $\angle 13$ _____ |

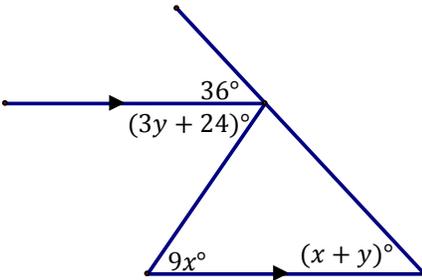
Part IV: Find the value of the variables.

1.



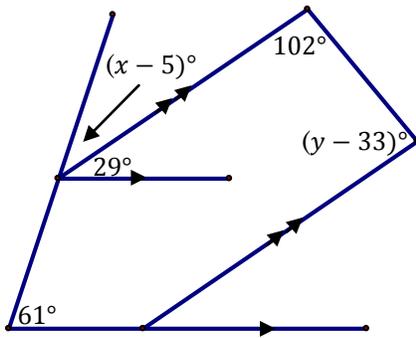
$x = \underline{\hspace{2cm}}$     $y = \underline{\hspace{2cm}}$

2.



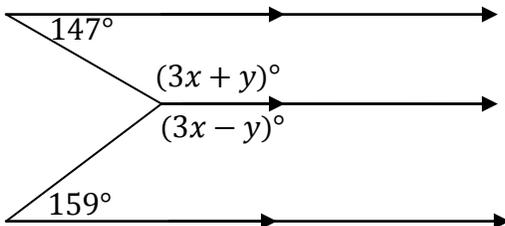
$x = \underline{\hspace{2cm}}$     $y = \underline{\hspace{2cm}}$

3.



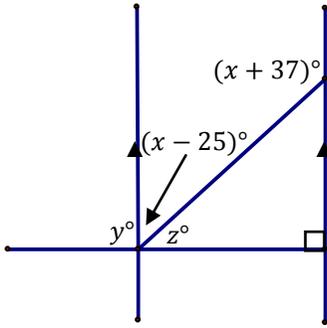
$x = \underline{\hspace{2cm}}$     $y = \underline{\hspace{2cm}}$

4.



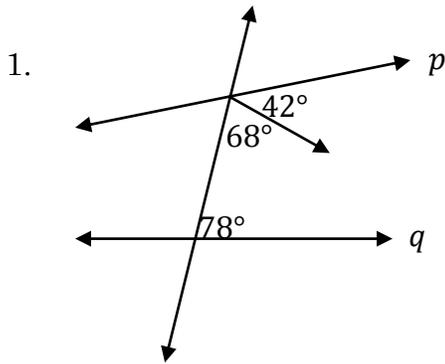
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5.

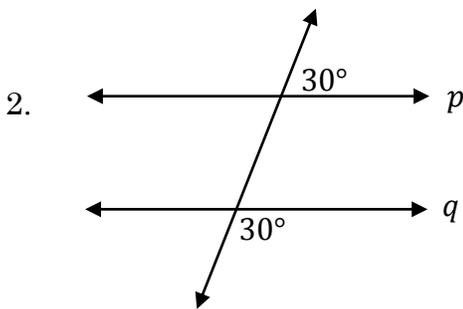


$x = \underline{\hspace{2cm}}$      $y = \underline{\hspace{2cm}}$      $z = \underline{\hspace{2cm}}$

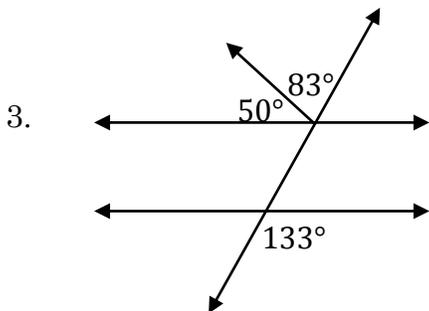
Part V. Is there enough information to state that lines  $p$  and  $q$  are parallel? If so, state the reason.



Yes \_\_\_\_\_ No \_\_\_\_\_  
 Reason (if necessary) \_\_\_\_\_  
 \_\_\_\_\_

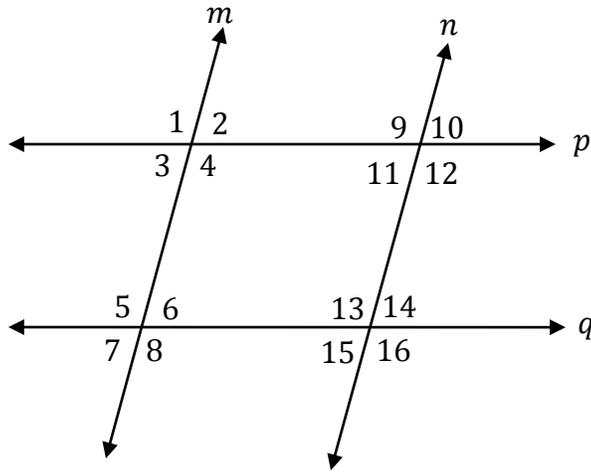


Yes \_\_\_\_\_ No \_\_\_\_\_  
 Reason (if necessary) \_\_\_\_\_  
 \_\_\_\_\_



Yes \_\_\_\_\_ No \_\_\_\_\_  
 Reason (if necessary) \_\_\_\_\_  
 \_\_\_\_\_

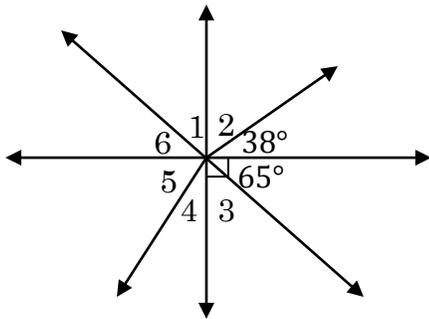
Part VI. Use the diagram and the given information to determine if  $m \parallel n$ ,  $p \parallel q$ , or neither.



1.  $\angle 3 \cong \angle 10$  \_\_\_\_\_
3.  $\angle 4 \cong \angle 11$  \_\_\_\_\_
5.  $\angle 12 \cong \angle 13$  \_\_\_\_\_
7.  $\angle 3 \cong \angle 14$  \_\_\_\_\_

2.  $\angle 1 \cong \angle 13$  \_\_\_\_\_
4.  $m\angle 11 + m\angle 13 = 180^\circ$  \_\_\_\_\_
6.  $m\angle 6 + m\angle 13 = 180^\circ$  \_\_\_\_\_

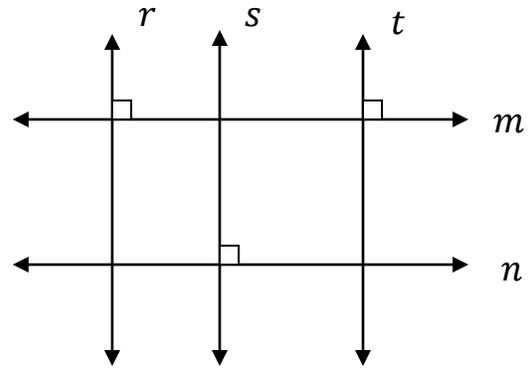
Part VII. Find the measure of the indicated angle.



$\angle 6 \cong \angle 5$

1.  $m\angle 1 =$  \_\_\_\_\_
2.  $m\angle 2 =$  \_\_\_\_\_
3.  $m\angle 3 =$  \_\_\_\_\_
4.  $m\angle 4 =$  \_\_\_\_\_
5.  $m\angle 5 =$  \_\_\_\_\_
6.  $m\angle 6 =$  \_\_\_\_\_

Part VIII. Use the diagram.



1. Is  $r \parallel s$ ?    Yes \_\_\_\_\_    No \_\_\_\_\_
2. Is  $m \parallel n$     Yes \_\_\_\_\_    No \_\_\_\_\_
3. Is  $r \parallel t$     Yes \_\_\_\_\_    No \_\_\_\_\_

Part IX. In the diagram,  $\overrightarrow{RS} \perp \overrightarrow{ST}$ . Find the value of  $x$ .

1.

$x = \underline{\hspace{2cm}}$

2.

$x = \underline{\hspace{2cm}}$

3.

$x = \underline{\hspace{2cm}}$

## Chapter 3 Review Solutions

### Part I:

- 1) Never
- 2) Never
- 3) Sometimes
- 4) Sometimes
- 5) Congruent
- 6) Supplementary
- 7) Congruent

### Part II:

- 1) Perpendicular
- 2) Parallel
- 3) Skew
- 4) Perpendicular
- 5) Parallel

### Part III:

- 1) Corresponding angles
- 2) Alternate exterior angles
- 3) None
- 4) Alternate interior angles
- 5) Vertical angles
- 6) Consecutive interior angles (same side interior)
- 7) Alternate exterior angles
- 8) None
- 9) Alternate interior angles
- 10) None
- 11) Linear Pairs
- 12) Consecutive Interior

### Part IV:

- 1)  $x = 21, y = 25$
- 2)  $x = 11, y = 25$  (system of equations)
- 3)  $x = 37, y = 111$
- 4)  $x = 9, y = 6$  (system of equations)
- 5)  $x = 84, y = 90, z = 31$

### Part V:

- 1) No, the sum of the angles is not 180 degrees
- 2) No, Corr. Angles are not congruent (one way to show)
- 3) Yes, alternate exterior angles converse (angles are congruent)

### Part VI:

- |  |  |
|--|--|
| 1) $m \parallel n$ Alt. Int. Converse    | 5) $p \parallel q$ Alt. Int. Converse    |
| 2) Neither-No transversal                | 6) $m \parallel n$ Consec. Int. Converse |
| 3) Neither- Need to be sup.              | 7) none- No Transversal                  |
| 4) $p \parallel q$ Consec. Int. Converse |  |

### Part VII:

- 1) 25
- 2) 52
- 3) 25
- 4) 25
- 5) 65
- 6) 65

### Part VIII:

- 1) Not enough information
- 2) Not enough information
- 3) Yes, both lines perpendicular to  $m$

### Part IX:

- 1)  $x = 18$
- 2)  $x = 12$
- 3)  $x = 15$