### Multiplication and Division are Inverse Operations

3, 12, 36

$$3 \times 12 = 36$$

$$12 \times 3 = 36$$

$$36 \div 12 = 3$$

$$36 \div 3 = 12$$

# "Inverse Operations" "Opposite Jobs"

They are inverse because you are taking a multiplication sentence and reversing it (not to be confused with the commutative property because we are not reordering factors - Division is **not** commutative).

#### Division

Just as multiplication is really a short-cut for repeated addition, division is really a short-cut for repeated subtraction.

 $15 \div 5 = ?$  means how many times can I subtract 5 from 15.

15

-<u>5</u> 1 time

10

-5 2 times

5

- 5 3 times

0

I subtracted 5 three times from 15 before I ended at 0, so  $15 \div 5 = 3$ 

You try:

b) 
$$15 \div 4 = ?$$

				4
rd:	Definition:	Examples:		· · · · · · · · · · · · · · · · · · ·
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division	repeated	15-5=3		
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	sharing fairly	15 1 time 10 2 times 5 3 times		я
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dividend	the number that is	8-2-4		;
	being divided	8-2=7		*
		218 2-4		2
×	16			e •
divisor	the number that is doing the division	8-2=4		t .
* · ·		2/8 = 4		
	1 2 3	78.		
quotient	the answer to a			
* *** *** *** *** *** *** *** *** ***	division problem	8-2=44		w ,
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As a Sentence	As a Fraction	Using the Symbol
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	<u>60</u> 12	
64-2 = 32		
		3 45
	48 4	
	<u>87</u>	
63 <del>5</del> 9 =		
		7 742

#### **Quotients and Remainders**

Divide.

1. 
$$7 \div 2 =$$

Copy and complete the input/Output table.

	INPUT	QUIPUT
	10 ÷ 3 ≒	
• •	27 ÷ 4 =	
	44 ÷ 9 =	
2	37 ÷ 5 =	
	34 + 6 =	
	17 + 2 =	
<u> </u>	74 ÷ 8 =	

As a Sentence	120	As a Fraction	Using the Symbol
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$49 \div 8 = 6\frac{1}{8}$	*		
6.1 Sec. 95			3)29
ats s	ě	3 <del>9</del> 7	
	8 30		9) 83
	ē ,,	4 5	
$74 \div 6 = 12\frac{1}{3}$	9		
			8)3
788		12 9	
$56 \div 12 = 4\frac{8}{12}$	1	1 × 1	
			7) 46
	*	<u>5</u>	
	-3/W.0-1	65 10	
	· · · · · · · · · · · · · · · · · · ·		12)6
$4 \div 12 = \frac{1}{3}$			

#### Division

Fill in the ? with the proper numeral or word phrase.

2. 
$$1)52$$

4. 
$$\frac{96}{0} = ?$$

5. 
$$\frac{24}{24} = ?$$

6. 
$$81)\frac{?}{81}$$

7. 
$$\frac{59}{0} = ?$$

8. 
$$73 \div 1 = ?$$

9. 
$$0)\frac{?}{78}$$

10. 
$$\frac{37}{1} = ?$$

11. 
$$\frac{0}{8} = 3$$

#### **Division**

Fill in the? with the proper numeral or word phrase.

1. 
$$\frac{22}{22} = ?$$

3. 
$$\frac{65}{0} = ?$$

5. 
$$54 \div 0 = ?$$

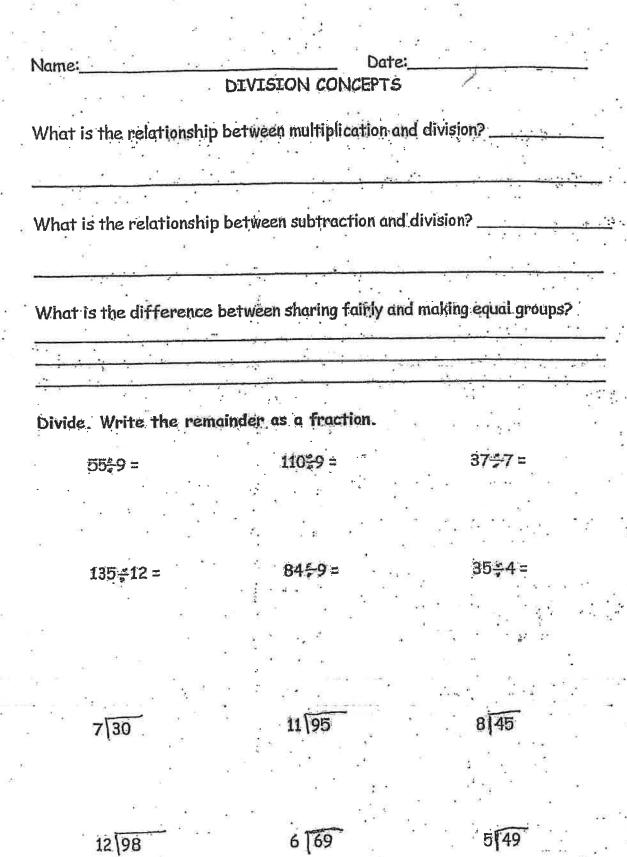
6. 
$$63)\overline{63}$$

7. 
$$\frac{23}{1} = ?$$

8. 
$$0)\frac{?}{42}$$

9. 
$$60 \div 1 = ?$$

10. 
$$\frac{75}{0} = ?$$



#### **Dividing with Multiples of 10**

- 1. Box the non-zero digits. Divide the number fact you know.
- 2. Cross out the zeroes using "dance partners"
- 3. The remaining zeroes are written in the answer.
- 4. Check!

$$72,000 \div 800 = 90$$

Check:  $800 \times 90 = 72,000$ 

Check:

Check:

Check:

Check:

$$5,250 \div 5 =$$
 \_\_\_\_\_\_  $6,360 \div 6 =$  \_\_\_\_\_\_

$$3,270 \div 30 =$$
\_\_\_\_\_

### Divide by Multiples of 10, 100, and 1,000

Look for Patterns When Dividing by Multiples of 10, 100, and 1,000

Estimate Find Find

18,000 ÷ 500  $335,000 \div 1 = 335,000$  $36 \div 4 = 9$ 

 $335,000 \div 10 = 33,500$  $15 \div 5 = 3$  $360 \div 4 = 90$ 

 $335,000 \div 100 = 3,350$  $15,000 \div 500 = 30$  $3.600 \div 4 = 900$ 

335,000 ÷ 1,000 = 335  $20 \div 5 = 4$  $36,000 \div 4 = 9,000$ 20,000 - 500 = 40

The quotient is between 30 and 40.

Divide. Use Mental Math.

1.  $810 \div 9$ 

2. 480 ÷ 60

3. 6,300 ÷ 900

 $4.4500 \div 500$ 

5.  $56,000 \div 700$ 

6. 40,000 ÷ 8,000 7. 210,000 ÷ 3,000 8: 540,000 ÷ 9,000

9. 800)24,000

10. 3,000)180,000 11. 600)300,000

.2. 9,000)360,000

#### **Problem Solving**

16. In Middletown, there is one principal for every 500 students. Middletown School District has 4,000 students. How many principals are there?

Show Your Work

Name:\_\_\_\_\_ Date
Mental Math!! Write the quotients ONLY!

Medical

10,500 ÷ 100 =

7,800 - 100 =

23,000 - 1000 =

640+20=

63,000 = 900 =

### -Math-Dividing with zeroes

II. 
$$770 \div 10 =$$

$$770,000 \div 100 =$$

$$77,000 \div 10 =$$

$$7,700 \div 100 =$$

#### **Estimating Quotients**

Think of MULTIPLES of the

$$180 \div 9 = 20$$

divisor (9) and round the dividend to that multiple. All remaining

Multiples of the Divisor (6): 6, 12, 18, 24, 30, 36, 42, 48

$$420 \div 6 = 70$$

Practice:

$$31,654 \div 8 =$$

- ROUND the DIVISOR to the largest place value
- Find the CLOSEST MULTIPLE to the new divisor.
- · Divide and add zeroes

$$270 \div 30 = 9$$

Practice:

Example: Estimate 325-8

325 is close to 320 and I know that I can divide 320 by 8.

### Estimate:

① 548 ÷ 5

② 627÷9

3 731 ÷12

4 275 ÷ 7

⑤ 316÷6

© 824÷13

7 185÷4

® 218÷3

#### **Estimate Quotients**

Estimate the quotient.

1. 6) 193

2. 5)439

3 9)3,621

4. 7)4,310

5. 8)78,452

6. 5)22,801

5) 7: 5) 266,113

8. 7)442,597

 $9.322 \div 6$ 

 $10.507 \div 4$ 

Enii. 6,828 ÷ 9,

12. 3,412 - 5

13. 12,461 ÷ 7

14. 65,135 ÷ 8

15. 588,117 ÷ 6

16. 528,117 ÷ 9

#### **Test Prep**

- 17. Luanne had 239 crafts to arrange as evenly as she could on 8 display tables. Which of these is a reasonable estimate of the number of crafts she put on each table?
  - A 3 crafts
- c 300 crafts
- B 30 crafts
- p 3,000 crafts
- 18. Jodie had 178 crafts to arrange on 8 display tables. Estimate how many she should put on each table to arrange them as evenly as possible. Tell what numbers you used for the dividend and the divisor.

#### Estimating Quotients HOMEWORK

Divide.

336÷8 = -

2,389÷42 =

62,895÷74=

5,178+58 =

412+52 =

7,439:89 =

821÷93 =

158÷77 =

265÷43 =

684÷81 =

9,175÷87 =

·358÷37 =

#### Remainders in Division

(Use the 4 step problem solving method)

#### 3 options:

1. Ignore it/Drop it

- the remainder is NOT NECESSARY in the answer OR it can't be used in the answer.

Sarah has \$50 to buy CDs. Each CD costs \$7. How many CDs can Sarah buy?

- 1. Let x = the number of CDs Sarah bought.
- 2. Div.  $50 \div 7 = x$

3.

$$50 \div 7 = 7 \frac{1}{7}$$

4. Sarah can buy 7 CDs.

You **drop** the remainder because you cannot buy 1/7 of a CD OR you cannot afford 8 CDs.

2. Keep the remainder

- the remainder is necessary for your answer to be correct.

Sean spent \$60 on candy. He bought 8 boxes to give as gifts. How much did each box of candy cost?

- 1. Let x = the cost per box of candy.
- 2. Div.  $60 \div 8 = x$

3.

$$60 \div 8 = 7 \frac{1}{2} = \$7.50$$

- \*\* When working with money, make sure you turn the remaining fraction into cents.\*\*
  - 4. Each box of candy costs \$7.50.

The remainder must **be kept** in the answer because it represents the exact amount of each box.

#### 3. Round the remainder

 the fractional part that is leftover must be rounded up to a whole number. The 5<sup>th</sup> grade students are going on a trip to Medieval Times. Buses need to be reserved for 84 students and 12 adults. Each bus holds 25 people. How many buses will be needed?

- 1. Let x = the number of buses needed
- 2. Add & Div.  $(84 + 12) \div 25 = x$

$$84 + 12 = 96$$

$$96 \div 25 = 3 \ 21/25$$

4. There needs to be 4 buses.

You **round** the remainder up so all the people can have a seat for the trip.

#### **Remainders in Division**

Drop/Ignore it	Keep it	Round up
<ul> <li>"full" or "whole"</li> <li>You have         something/object you         can't break into         fractional parts</li> <li>Remainder is not         needed in your final         answer.</li> </ul>	<ul> <li>Usually deals with money \$\$</li> <li>You can break whatever it is into fractional parts.</li> <li>Exact amount is given- no more, no less.</li> </ul>	<ul> <li>You have something/ object that you can't break into fractional parts</li> <li>You need the remaining parts (numerator in the fraction) in your answer.</li> </ul>
Examples:	Example:	Example:
Mrs. Smith put books into boxes. She had 32 books. Each box held 5 books. How many full boxes did she pack?	Sean spent \$9 on dog bones. He bought 6 bones. How much did each bone cost?	90 people went on a bus to the park. Each bus held 25 people. How many buses did they need to order?

Division	Problems	/Interpreting	Remainders
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Use the Four Step Problem Solving Method.

1. Mr. Lou is setting up benches for the kindergarten play. Each bench can seat 7 people. 66 people are expected to attend. How many benches does he need to set up?

What do you do about the remainder?

Keep it

Drop It

Round up

Why?

2. Team membership for the local soccer league is \$50. The team is scheduled to play 8 games during the season. What is the cost per game?

What do you do about the remainder? Why?

3.	Rebecca	and her	three	sister	s bought	their mo	ther a shirt	for l	ner
	birthday.	. It cost	t \$42,	which	included	the tax.	How much	did	each
	sister ha	ve to co	ntribu	ite tow	ards the	gift?			

What do you do about the remainder? Why?

4. Mary is excited to go to FYE to buy some DVDs. They are having a great sale where all DVDs are selling for \$9 each. How many DVDs can she buy with \$30?

What do you do about the remainder? Why?

5.	The fifth grade teachers are organizing the buses for our class trip to
	Medieval Times. 110 students, teachers, and class parents will be
	attending the trip. How many buses should be reserved if each bus
	can seat 12 people?

What do you do about the remainder? Why?

6. How many times will I need to put the yardstick down if I need to measure 16 feet?

What do you do about the remainder? Why?



Estimate Divide

Check

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ESTIMATE FIRST, then compute. Use the TRADITIONAL METHOD OF DIVISION to calculate the answers to the following problems.

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## TRADITIONAL METHOD HOMEWORK EXAMPLE: Traditional Method

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Estimate Divide

Check

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### Zero in the Quotient

Use the TRADITIONAL METHOD OF DIVISION to calculate the answers to the following problems.
ESTIMATE FIRST, then compute.

Why my the party

stimate Divide Check

## Short Cut Division

- Use when you have ONE digit divisor ONLY; the size of the dividend does not matter.
- The process where you divide and record the remainders horizontally.
- Multiplication and subtraction steps are done mentally. The remainder is written as a subscript and placed before the next digit.

ESTIMATE FIRST, then compute. Use the SHORT METHOD OF DIVISION to calculate the answers to the following problems.

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9)1127

8)6754

9)5686

4)3987

Name:

# 

Divide using the Short Cut method.

Divide using the Traditional Method.

# Divide using the SHORT CUT METHOD.

# Divide

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Solve the following problems. Be sure to state what to do with the remainder. Solve using the 4-Step method,

1. David and his 6 friends shared 491 baseball cards. How many cards did each friend get? What do you do with the remainder? Why?

2. Jon and 7 friends bought a Valentine's gift for Jon's mom. The gift cost \$140 including tax. How much did each have to pay for the gift? What do you do with the remainder? Why?

3. There were 350 cars washed during the day at the car wash:
Fifteen attendants were on hand to wash the cars. How many
cars did each attendant wash? What does the remainder
represent? What do you do with it? Why?

#### Word Problems

Solve the following word problems using the 4 Step Problem Solving Plan.

1. Mrs. Barbag is packing cupcakes for her niece's birthday party. She has made 205 cupcakes. She can put 24 cupcakes in each box. How many boxes does she need to pack all of the cupcakes?

2. Mr. Diegnan bought 4 books for \$2.95 each and a board game for \$15.95. He paid with a \$50.00 bill. How much change did he get?

3. Mrs. Picolli is packing up books in the library. She has 431 books to pack. The boxes each hold 36 books. After she boxes up as many books as she can, how many books will she have left over?

4. For eight days the track team ran 16 laps. If there were 52 students on the track team, how many laps did the students run in all?

5. The bookstore sold 4,491 magazines from January through the end of September. If the same amount of magazines were sold each month, how many magazines were sold during April?

6. Twenty-seven famous authors visit the bookstore each year. If a total of 9,369 books were signed by authors last year, about how many books did each author sign?

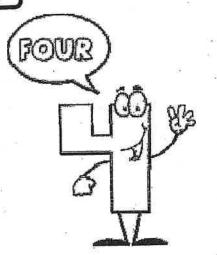
7. Each day the customers in the bookstore read a total of 6,048 pages. There are 48 regular customers every day who go to the bookstore to have a cup of coffee and read. If each regular customer reads the same number of pages each day, how many pages does one regular customer read per day?

8. The bookstore receives 2,014 new books each month. If the same amount is received each month for 1 year, about how many books will be received in all?

# 4-Step Order of Operations- Step-by-Step Lesson

Find the end value of the problem.

$$7 + 4 \times (4 + 1) \div 5 - 4$$



Explanation: We need to be reminded about the order in which attack a problem like this. The acronym PEMDAS indicates the order.

We process calculations in this order:

Parentheses, Exponents, (Multiplication, Division), Addition, and Subtraction

Note the parentheses around multiplication and division. That is because those operations are at the same level. When deciding to divide or multiply on a step, we process the calculation to the left first. Division and multiplication is processed left to right.

Step 
$$\alpha: 7+4\times (4+1)\div 5-4=7+4\times 5\div 5-4$$

**Parentheses** 

Step b: 
$$7 + 4 \times 5 \div 5 - 4 = 7 + 20 \div 5 - 4$$

$$= 7 + 20 \div 5 - 4$$

Multiplication (Left)

Step c : 
$$7 + 20 \div 5 - 4$$

$$= 7 + 4 - 4$$

Division

$$= 11 - 4$$

Step e: 11-4

Name \_\_\_\_\_

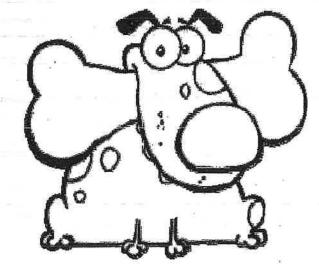
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#### 4-Step Order of Operations- Guided Lesson

Complete the following problems:

1) 
$$10 - 12 \div (8 - 4) \times 5 + 7$$



2) 
$$5 + 8 \times (4+5) \div 4-3$$

# 4-Step Order of Operations- Independent Practice Worksheet

Complete all the problems.

1. 
$$8 + 5 \times (7 + 8) \div 3 - 4$$

2. 
$$5 + 11 \times (4 + 5) \div 3 - 1$$

$$3.9 + 9 \times (2 + 4) \div 3 - 2$$

$$4.8 + 6 \times (3 + 3) \div 3 - 7$$

6. 
$$45 - 8 \div (4 - 2) \times 9 + 10$$

7. 
$$28 - 15 \div (8 - 3) \times 8 + 6$$

10. 
$$55 - 64 \div (16 - 8) \times 6 + 9$$



Name \_\_\_\_\_

Date \_\_\_\_\_

#### 4-Step Order of Operations - Matching Worksheet

41

Write the letter of the answer that matches the answer to each problem.

1. 
$$18 + 9 \times (5 + 4) \div 3 - 5$$

$$2.21 + 7 \times (4 + 4) \div 4 - 10$$

$$3.15 + 21 \times (2 + 2) \div 12 - 13$$

5. 
$$31 + 35 \times (3 + 3) \div 21 - 7$$

6. 
$$30 - 32 \div (6 - 2) \times 3 + 12$$

$$------ 7. 150 - 72 \div (24 - 16) \times 15 + 7$$

9. 
$$40 - 100 \div (50 - 30) \times 4 + 40$$

\_\_\_\_\_ 10. 85 - 20 
$$\div$$
 (30 - 20) x 8 + 15

Name

Score:

42

Teacher

Date:

## **Order of Operations**

$$6)10 \div 2 + 18 \times 4$$

$$7)14 \times 12 \div 6 - 3$$

10) 
$$5 + 10 \div 5 \times 14$$

Name:

Score:

Date:

acher

### Order of Operations

8) 
$$10 \times 6 \times (\frac{9-6}{6-9})$$

9) 
$$(11+55-6)\div 6$$

Volume =  $1 \times w \times h$ 



5 q.

 $5 \times 9 \times n = 90$ 

 $45 \times n = 90$ 

What, when multiplied by 45, equals 90?

n = 2

Complete the table with the missing measurements.

	Length	Width	Height	Volume
1.	· 4 inches	12 inches		48 cubic inches
2.	6 feet		3 feet	36 cubic feet
3.		9 centimeters	2 centimeters	54 cubic centimeters
4.	2 meters	2 meters	2 meters	
5.	4 inches		3 inches	84 cubic inches
6.	3 yards	6 yards		36 cubic yards
7.	9 inches	7 inches	7 inches	
8.		13 centimeters	4 centimeters	416 cubic centimeters
<b>9.</b>	3 feet		8 feet	192 cubic feet
10.	,6 millimeters	5 millimeters	9 millimeters	

I can use formulas to find the volume of rectangular prisms.

Name\_

5:MD.5c

You can find the volume of more complex figures using addition.

First, split the shape into two rectangular prisms.

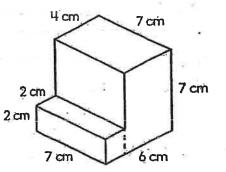
Then, find the volume of each prism.

2 cm × 2 cm × 7 cm = 28 cubic cm

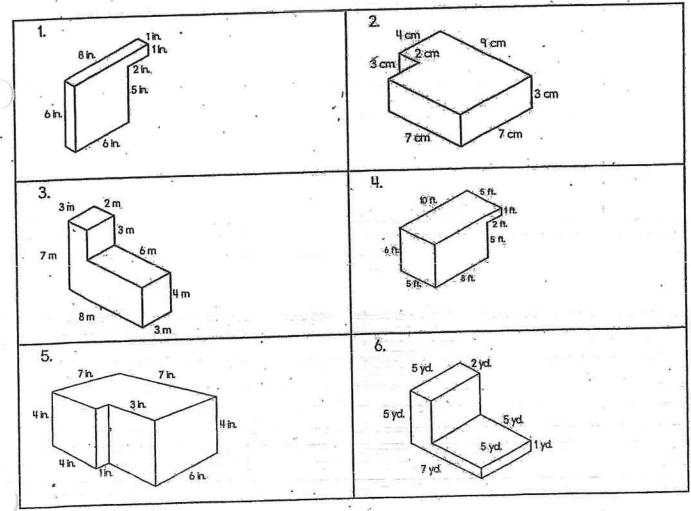
<sup>2</sup> 4 cm × 7 cm × 7 cm = 196 cubic cm

Finally, add the two volumes together.

28 cubic cm + 196 cubic cm = 224 cubic cm



Find the volume of each figure.



- ☐ I understand that volume can be added.
  - I can find the volume of complex rectangular prisms.

### Solve the following problems.

1. Volume = 84 cm.<sup>3</sup>
Height = 4 cm
Length = 3 cm
Value of the width?

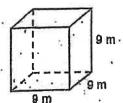
- Volume = 72 ft.<sup>3</sup>
   Height = 2 ft.
   Width = 9 ft.
   Value of the Length = ???
- 3. Joe's toolbox is 20 inches long, 12 inches wide, and 10 inches high. Find the volume of the toolbox.

4. The volume of a crate is 288 cubic feet. If the width is 4 feet and the height is 8 feet, how high is the crate?

5. A cube has a height of 7 inches. What is the volume of the cube?

6. A rectangular box has a height of 6 inches, a width of 10 inches, and a length of 11 inches. What is the volume of the box?

3.





What is special about the length, width, and height in this example? What is the name of this three-dimensional figure?

4. A rectangular solid has a volume of 36 cubic inches (in.³). If the length is 3 inches, what are possible combinations of values for the width and the height of the figure?

5. A rectangular solid has a volume of 60 cubic feet (ft.3). If the width is 4 feet, what are possible combinations of values for the height and the length of the figure?

7. Bill has a rectangular prism completely filled with 132 unit cubes. What are possible values for the length, width and height of the rectangular prism? Explain your thinking.

8. Pam has a rectangular prism completely filled with 108 unit cubes. What are possible values for the length, width and height of the rectangular prism? Explain your thinking.

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